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# Comments on general gauge mediation

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ABSTRACT: There has been interest in generalizing models of gauge mediation of supersymmetry breaking. As shown by Meade, Seiberg, and Shih (MSS), the soft masses of general gauge mediation can be expressed in terms of the current two-point functions of the susy-breaking sector. We here give a simple extension of their result which provides, for general gauge mediation, the full effective potential for squark pseudo-D-flat directions. The effective potential reduces to the sfermion soft masses near the origin, and the full potential, away from the origin, can be useful for cosmological applications. We also generalize the soft masses and effective potential to allow for general gauge mediation by Higgsed gauge groups. Finally, we discuss general gauge mediation in the limit of small F-terms, and how the results of MSS connect with the analytic continuation in superspace results, based on a spurion analysis.

KEYWORDS: Supersymmetry Breaking, Supersymmetric Effective Theories.



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### 1. Introduction

A standard framework for building potentially realistic supersymmetric models is based on theories of the form

$$\mathcal{L} = \mathcal{L}_1 + \mathcal{L}_2 + \mathcal{L}_{\text{int}}, \tag{1.1}$$

where  $\mathcal{L}_1$  is the MSSM or some extension,  $\mathcal{L}_2$  is the hidden sector with broken supersymmetry, and the  $\mathcal{L}_{int}$  interactions couple them. In gauge mediation [1-11], the gauge interactions are the most important part of  $\mathcal{L}_{int}$ . This scenario has been extensively studied for simple, weakly coupled, hidden sectors  $\mathcal{L}_2$ . It is potentially interesting to extend such results to more complicated hidden sectors, including those which are not necessarily weakly coupled, see e.g. [6, 12-15]. A general framework that can accommodate this scenario was considered in [16], where it was shown that the soft masses of MSSM gauginos and sfermions, to leading order in the  $\mathcal{L}_{int}$  gauge interactions, can be expressed in terms of the  $\mathcal{L}_2$  current correlation functions. Related following works include [17-22].

In this short note, we extend the results of [16] to compute the full effective potential for the sfermion fields. Expanding the effective potential around the origin gives the sfermion masses. The form of the effective potential far from the origin can be of interest for cosmological models, as in [23]. When the susy-breaking/messenger sector  $\mathcal{L}_2$  is weakly coupled and expanded for small susy-breaking F-terms, our general effective potential reduces to that obtained in [23]. We also express the full effective potential, generalized to allow for the possibility that the messenger gauge group is Higgsed. Expanding around the origin, this gives the gaugino and sfermion masses for general Higgsed gauge mediation. When the susy-breaking sector  $\mathcal{L}_2$  is weakly coupled, these results reduce to those recently obtained in [24] for Higgsed gauge mediation. Finally, we discuss a relation between these current-correlator results and the discussion in [25] of the 1PI effective action and RG running. We discuss the results of [16] in terms of superspace and show how a spurion analysis reproduces the results obtained by analytic continuation in superspace [26, 25] in the limit of small supersymmetry breaking. The organization of this paper is as follows. In section 2, we give a brief review of General Gauge Mediation [16]. In section 3, the full effective potential is presented in this formalism, and the generalization to Higgsed gauge groups is discussed. In section 4, superspace techniques [26, 25] are used to extract results for small F-term breaking. The main observations of section 4 were independently obtained in the recent work [22]

# 2. Review of general gauge mediation [16]

In supersymmetric gauge theories, the gauge supermultiplet  $\mathcal{V}$  couples to the current supermultiplet,  $\mathcal{J}$ , which is a real linear superfield satisfying  $D^2 \mathcal{J} = \bar{D}^2 \mathcal{J} = 0$ . In components,

$$\mathcal{J} = J + i\theta j - i\bar{\theta}\bar{j} - \theta\sigma^{\mu}\bar{\theta}j_{\mu} + \frac{1}{2}\theta\theta\bar{\theta}\bar{\sigma}^{\mu}\partial_{\mu}j - \frac{1}{2}\bar{\theta}\bar{\theta}\theta\sigma^{\mu}\partial_{\mu}\bar{j} - \frac{1}{4}\theta\theta\bar{\theta}\bar{\theta}\Box J, \qquad (2.1)$$

with  $\partial^{\mu} j_{\mu} = 0$  and the other components unconstrained. The gauge interactions couple to  $\mathcal{J}$  as

$$\mathcal{L}_{\rm int} \supset 2g \int d^4\theta \mathcal{J}\mathcal{V} + \ldots = g(JD - \lambda j - \bar{\lambda}\bar{j} - j^{\mu}V_{\mu}) + \ldots, \qquad (2.2)$$

where the component expansion is in Wess-Zumino gauge. As shown in [16], the diagrams of figure 1, which give the soft supersymmetry breaking masses of the visible sector, can be expressed in terms of the hidden-sector current-current two-point functions. Lorentz invariance and current conservation fix the form of the Euclidean momentum-space twopoint functions of these fields as (dropping a  $(2\pi)^4 \delta^{(4)}(0)$ ):

$$\langle J(p)J(-p)\rangle = \widetilde{C}_0(p^2/M^2) \tag{2.3}$$

$$\langle j_{\alpha}(p)\bar{j}_{\dot{\alpha}}(-p)\rangle = -\sigma^{\mu}_{\alpha\dot{\alpha}}p_{\mu}\widetilde{C}_{1/2}(p^2/M^2)$$
(2.4)

$$\langle j_{\mu}(p)j_{\nu}(-p)\rangle = -(p^{2}\eta_{\mu\nu} - p_{\mu}p_{\nu})\widetilde{C}_{1}(p^{2}/M^{2})$$
(2.5)

$$\langle j_{\alpha}(p)j_{\beta}(-p)\rangle = \epsilon_{\alpha\beta}M\tilde{B}_{1/2}(p^2/M^2)$$
(2.6)

for some functions,  $\tilde{C}_0$ ,  $\tilde{C}_{1/2}$ ,  $\tilde{C}_1$ , and  $\tilde{B}_{1/2}$ . If supersymmetry were unbroken,  $\tilde{C}_0 = \tilde{C}_{1/2} = \tilde{C}_1$ , and  $\tilde{B}_{1/2} = 0$ . Here M is a mass scale in the problem. We are interested in these twopoint functions in the hidden sector, where supersymmetry is broken. The  $\tilde{C}_{j=0,1/2,1}$  also depend on a UV cutoff, which is needed to regulate the Fourier transform from position space to momentum space, as

$$\widetilde{C}_j(p^2/M^2) = 2\pi^2 c \log(\Lambda/M) + \widetilde{C}_j^{\text{finite}}(p^2/M^2)$$
(2.7)

where only the finite terms  $\widetilde{C}_{j}^{\text{finite}}$  depend on j when supersymmetry is spontaneously broken. Also, in this case,  $\widetilde{B}_{1/2}$  is independent of  $\Lambda$  [16].

To  $\mathcal{O}(g^2)$ , the hidden sector then contributes to the effective action for the gauge supermultiplet fields as [16]

$$\delta \mathcal{L}_{\text{eff}} = \frac{1}{2} g^2 \widetilde{C}_0(0) D^2 - g^2 \widetilde{C}_{1/2}(0) i \lambda \sigma^\mu \partial_\mu \bar{\lambda} - \frac{1}{4} g^2 \widetilde{C}_1(0) F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} g^2 (M \widetilde{B}_{1/2}(0) \lambda \lambda + c.c.) + \dots$$
(2.8)



Figure 1: Diagram D1 gives mass to gauginos and is expressible in terms of the function  $\tilde{B}_{1/2}$ . Diagrams D2-D5 contribute to the masses of sfermions and involve the functions  $\tilde{C}_0$ ,  $\tilde{C}_{1/2}$ , and  $\tilde{C}_1$ , respectively.

The divergent part of (2.7) is the hidden-sector contribution to the gauge beta function:

$$\delta \frac{dg}{d\ln\mu} = \frac{g^3}{16\pi^2} (2\pi)^4 c, \qquad (2.9)$$

with c > 0.

The diagrams of figure 1, which give masses to the visible sector gauginos and sfermions were evaluated in [16] in terms of the current correlator functions as

$$M_{a} = g_{a}^{2} M \widetilde{B}_{1/2}^{(a)}(0),$$
  

$$m_{\widetilde{f}}^{2} = g_{1}^{2} Y_{f} \xi + \sum_{a} g_{a}^{4} c_{2}(a_{f}) A_{a}$$
  

$$A_{a} \equiv -\int \frac{d^{4} p}{(2\pi)^{4}} \frac{1}{p^{2}} \left( 3 \widetilde{C}_{1}^{(a)}(p^{2}/M^{2}) - 4 \widetilde{C}_{1/2}^{(a)}(p^{2}/M^{2}) + \widetilde{C}_{0}^{(a)}(p^{2}/M^{2}) \right).$$
(2.10)

The index a runs over the gauge groups, f runs over the sfermions, Y is the hypercharge, and  $\xi$  is an FI parameter. Note that the integrand of  $A_a$  has the form of a super-trace<sup>1</sup> and, without additional information or constraints, it looks like it can have either sign.

<sup>&</sup>lt;sup>1</sup>A related expression appears in [23] for the messenger  $m_{\text{mess}}^2$ , in the context of models with a separate messenger sector (where it was argued that perturbative estimates based on naive dimensional analysis should be essentially reliable even for strongly coupled susy-breaking sectors).



Figure 2: Diagrams D6, D7, and D8 give contributions to the effective potential involving the functions  $\widetilde{C}_0$ ,  $\widetilde{C}_{1/2}$ , and  $\widetilde{C}_1$ , respectively.

## 3. The effective potential and higgsed gauge mediation

The sfermions of the visible sector generally have tree-level D-flat directions. With supersymmetry breaking, these directions are lifted first by the two-loop effective potential. Near the origin, this effective potential reduces to the sfermion mass terms. Far from the origin, the effects of susy breaking shut off, and the effective potential becomes very flat. The full effective potential can be of interest for cosmological models and was computed in [23], to leading order in small F-terms, for the case of a weakly coupled messenger sector. Here we give a simple expression for the full effective potential, for arbitrary F-terms, in general gauge mediation.

The effective potential is computed from the diagrams of figure 2. For simplicity, we quote the result for a single U(1) gauge group — the more general case is similar. We find that the effective potential is simply

$$V_{\rm eff}(m_W^2) = \frac{g^2}{2} \int \frac{d^4p}{(2\pi)^4} \frac{p^2}{p^2 + m_W^2} \left( 3\widetilde{C}_1(p^2/M^2) - 4\widetilde{C}_{1/2}(p^2/M^2) + \widetilde{C}_0(p^2/M^2) \right).$$
(3.1)

Here  $m_W = 2g|\langle Q \rangle|$  is the mass of the vector multiplet, where  $\langle Q \rangle$  is along a direction which would have been D-flat if not for the supersymmetry breaking. The terms in (3.1) simply come from contracting the massive vector multiplet propagators with the appropriate current-current correlator, e.g. from diagram D8 we have (in Euclidean space)

$$\frac{g^{\mu\nu}}{p^2 + m_W^2} (p^2 \eta_{\mu\nu} - p_\mu p_\nu) \widetilde{C}_1(p^2/M^2) = \frac{p^2}{p^2 + m_W^2} 3\widetilde{C}_1(p^2/M^2).$$
(3.2)

Diagram D7 is similar, with the massive gaugino propagator contracted with (2.4). Diagram D6, with the auxiliary field D, requires a bit more attention because it mixes with a real scalar, C, of the massive gauge multiplet:

$$\Delta_{CD} = \begin{pmatrix} 1 & m_W \\ m_W & -p^2 \end{pmatrix}^{-1} = \frac{1}{p^2 + m_W^2} \begin{pmatrix} p^2 & m_W \\ m_W & -1 \end{pmatrix},$$
(3.3)

so the *D*-field propagator is  $p^2/(p^2 + m_W^2)$ , which then yields the  $\widetilde{C}_0$  contribution to (3.1).

Let us now verify that our general effective potential (3.1) reduces to the sfermion  $m_{\tilde{f}}^2$ in (2.10), when expanded around the origin. Consider

$$m_{\tilde{f}}^2 = \frac{\partial V_{\text{eff}}}{\partial |\langle Q \rangle|^2} = -2g^4 \int \frac{d^4p}{(2\pi)^4} \frac{p^2}{(p^2 + m_W^2)^2} \left( 3\tilde{C}_1(p^2/M^2) - 4\tilde{C}_{1/2}(p^2/M^2) + \tilde{C}_0(p^2/M^2) \right). \tag{3.4}$$

Evaluating this for  $m_W^2 = 0$  indeed reduces to the expression of [16].

One can also verify that the general result (3.1) reduces to the effective potential obtained in [23], for the special case of weakly coupled hidden sector (using the expressions for  $\tilde{C}_j$  in the appendix of [16]), when evaluated to leading order in small F-terms. The case of weakly coupled  $\mathcal{L}_2$  sector, for general (not necessarily small) F-terms, can also be compared and verified with the result obtained using the formulae of [27].

With no additional work, we can extend our result to allow for the possibility of Higgsed gauge mediation. We simply replace  $m_W^2 \to m_W^2 + 4g^2 |\delta Q|^2$  in (3.1), and keep the  $m_W \neq 0$ . Expanding to  $\mathcal{O}(|\delta Q|^2)$ , the result (3.4), with  $m_W \neq 0$ , gives the sfermion  $m_{\tilde{f}}^2$  in general Higgsed gauge mediation. For the case of weakly coupled messengers, it can be verified that the result (3.4) indeed reduces to the results obtained in [24] for Higgsed gauge mediation.

# 4. Superspace techniques and analytic continuation in superspace

In the context of weakly coupled gauge mediation, there are nice methods [26, 25] which allow multi-loop quantities, including sfermion masses, to be reduced to one-loop quantities at leading order in small supersymmetry breaking F-terms. Fields  $\varphi$  and  $\tilde{\varphi}$  of the susybreaking sector get susy-split masses via  $W = X\varphi\tilde{\varphi}$ , where X is a spurion (background) chiral superfield  $X = M + \theta^2 F$ . The results follow from imposing the constraints of holomorphy in X on the effective action. The results are limited to leading order in small F, because terms higher order in F arise from higher super-derivative terms in superspace, which are not considered. Taking  $x \equiv |F/M^2| \ll 1$ , the methods determine the soft masses to  $\mathcal{O}(x)$ .

The methods of [26, 25] extend immediately to general gauge mediation. The gaugino masses come from the holomorphic gauge coupling  $\tau = \theta/2\pi + 4\pi i/g^2$ , which is a holomorphic function  $\tau(X)$  below the scale X thanks to the threshold matching and the contribution (2.9) of the hidden sector to the beta function there. The sfermion masses come from the one-loop  $\mathcal{O}(g^2)$  contribution to  $Z_Q(X, \bar{X})$ , which depends of X again via the gauge coupling. This gives  $\beta_{g_a}^{(1)}$ , and  $m_{\tilde{f}}^2 \sim \gamma_{\tilde{f}}^{(1)} \Delta \beta_{g_a}^{(1)}$ , in terms of the beta-function coefficient c in (2.9) and (2.7):

$$M_a \approx \frac{g_a^2}{16\pi^2} (2\pi)^4 c_a \frac{F}{M},$$
  

$$m_{\tilde{f}}^2 \approx \sum_a 2c_2(a_f) \frac{g_a^4}{(16\pi^2)^2} (2\pi)^4 c_a \Big| \frac{F}{M} \Big|^2.$$
(4.1)

In this small F limit, the masses  $m_{\tilde{f}}^2$  are manifestly positive.

The simple expressions (4.1) motivate a parallel spurion analysis of the current correlation functions, to connect with the results of [16], quoted above in (2.10), when expanded in small F. In the small-F limit, we have  $\tilde{C}_j \approx \tilde{C}_{susy}$ , independent of j = 0, 1/2, 1. To leading order in small F, we find that the susy-breaking quantities appearing in the soft masses (2.10) can be expressed, for all  $p^2/M^2$ , as

$$-M\widetilde{B}_{1/2}(p^2/M^2) = F\frac{\partial}{\partial M}\widetilde{C}_{\text{susy}}(p^2/M^2) + \mathcal{O}(F|F|^2/M^6), \qquad (4.2)$$

and

$$3\tilde{C}_{1}(p^{2}/M^{2}) - 4\tilde{C}_{1/2}(p^{2}/M^{2}) + \tilde{C}_{0}(p^{2}/M^{2}) = 2\frac{|F|^{2}}{p^{2}}\frac{\partial^{2}}{|\partial M|^{2}}\tilde{C}_{susy}(p^{2}/M^{2}) + \mathcal{O}(|F|^{4}/M^{8}),$$
(4.3)

It is easily verified that these identities are indeed satisfied for the particular case of weakly coupled messengers, by expanding for small F/M the explicit expressions for  $\widetilde{C}_j$ and  $\widetilde{B}_{1/2}$  in the appendix of [16]. The identities (4.2) and (4.3) were independently derived, with the same motivation, in a recent paper of Distler and Robbins [22].

One approach is to prove (4.2) and (4.3) directly in terms of the current correlation functions, first enforcing the supersymmetric and current conservation Ward identities, and introducing the supersymmetry breaking spurion via  $M \to X = M + \theta^2 F$ . The first step is simplified by writing the current supercorrelators in superspace. In particular, the current 2-point functions for unbroken supersymmetry are given by an immediate generalization of the conformal result in [28] to the nonconformal case:

$$\langle \mathcal{J}(z_1)\mathcal{J}(z_2)\rangle = \frac{C(M^4 x_{\overline{2}1}^2 x_{\overline{1}2}^2)}{x_{\overline{2}1}^2 x_{\overline{1}2}^2}, x_{\overline{1}2}^{\mu} = x_1^{\mu} - x_2^{\mu} - i\theta_1 \sigma^{\mu} \bar{\theta}_1 - i\theta_2 \sigma^{\mu} \bar{\theta}_2 + 2i\theta_2 \sigma^{\mu} \bar{\theta}_1.$$
 (4.4)

Instead of introducing the spurions in (4.4), we will now do it in terms of the 1PI effective action, since that is anyway more directly relevant for extracting the implications for gauge mediation.

Consider first the 1PI effective action to  $\mathcal{O}(F^0)$ , neglecting supersymmetry breaking effects. We follow the notation of [25]. There is a term which gives the gauge kinetic terms and higher derivative terms associated with running:

$$\Gamma_{1PI} \supset \int d^4p \int d^2\theta \frac{1}{2} \gamma(p^2) W^{\alpha} W_{\alpha} + h.c.$$
  
=  $\int d^4p \int d^4\theta \ \gamma(p^2) W^{\alpha} \frac{D^2}{-8p^2} W_{\alpha} + h.c..$  (4.5)

The expression on the second line is equivalent if supersymmetry is unbroken, and will be the one to use once supersymmetry breaking is introduced. There are also terms in the effective action involving the visible sector matter, e.g.

$$\Gamma_{1PI} \supset \int d^4p \int d^4\theta \zeta(p^2) (Q^{\dagger} e^V Q + \widetilde{Q}^{\dagger} e^{-V} \widetilde{Q}).$$
(4.6)

Classically,  $\gamma(p^2) = 1/g^2$ , and one can define the quantum running couplings and Z-factors as  $\gamma(p^2)|_{p^2=-\mu^2} = 1/g^2(\mu^2)$ , and  $\zeta_f(p^2)|_{p^2=-\mu^2} = Z_f(\mu^2)$ . To  $\mathcal{O}(g^2)$ , the hidden sector current-current two-point functions contribute

$$\delta\gamma(p^2/M^2) = g^2 \widetilde{C}_{\text{susy}}(p^2/M^2). \tag{4.7}$$

The leading term in the low-momentum expansion of (4.5) then gives the terms (2.8) in the effective Lagrangian (in the susy limit). We are here interested in the relation (4.7) for general  $p^2$ .

We now introduce the supersymmetry breaking spurion via  $M \to X = M + \theta^2 F$ . To  $\mathcal{O}(|F|^2)$ , the relation (4.7) is simply preserved, and both sides pick up  $\theta$  components. The expression on the second line of (4.5) yields

$$\Gamma_{1PI} \supset \frac{1}{2} \int d^4p \int d^2\theta \, (\gamma(p^2)|_0 + \theta^2 \gamma(p^2)|_{\theta^2}) W^{\alpha} W_{\alpha} + h.c. + \int d^4p \, \gamma(p^2)|_{\theta^2 \bar{\theta}^2} \frac{\lambda \sigma^{\mu} p_{\mu} \bar{\lambda}}{-p^2}$$
(4.8)

where, according to (4.7) with the spurions, we have

$$\gamma(p^2)|_{\theta^2} = g^2 F \frac{\partial}{\partial X} \widetilde{C}_{\text{susy}}(p^2/|X|^2) \bigg|_{X=M}, \qquad \gamma(p^2)_{\theta^4} = g^2 |F|^2 \frac{\partial^2}{|\partial X|^2} \widetilde{C}_{\text{susy}}(p^2/|X|^2) \bigg|_{X=M}.$$
(4.9)

The  $\gamma(p^2)|_{\theta^2}$  term in (4.8) is generated in the effective action by the nonsupersymmetric analog of (4.7), by non-supersymmetric current two-point functions:

$$\gamma(p^2)|_{\theta^2} = -g^2 M \widetilde{B}_{1/2}(p^2/M^2) - \mathcal{O}(F|F|^2).$$
(4.10)

On the r.h.s. we keep only the  $\mathcal{O}(F)$  term, and the factor of -M is as in (2.8). Comparing (4.9) and (4.10) gives the relation (4.2).

Likewise, the  $\gamma(p^2)|_{\theta^4}$  term in (4.8) is generated by the non-supersymmetric analog of (4.7), from supersymmetry breaking contributions of the current-current two-point functions to the effective action. Indeed, it is easily seen, as in (2.8), that a supersymmetry breaking shift of  $\tilde{C}_{1/2}(p^2/M^2)$  will generate the  $\gamma(p^2)|_{\theta^4}$  term in (4.8). Since this supersymmetry breaking term comes from such a  $\tilde{C}_{1/2}$  shift relative to  $\tilde{C}_0$  and  $\tilde{C}_1$ , it is generated only by the supertrace:

$$\frac{1}{p^2}\gamma(p^2)|_{\theta^4} = \frac{g^2}{2} \left( \widetilde{C}_0(p^2/M^2) - 4\widetilde{C}_{1/2}(p^2/M^2) + 3\widetilde{C}_1(p^2/M^2) \right) - \mathcal{O}(|F|^4)), \quad (4.11)$$

where only terms to  $\mathcal{O}(|F|^2)$  are kept on the r.h.s. This relation essentially appears already in [25] (in terms of the gauge field effective propagators), where it was noted to follow from considering all the possible contributing terms involving the spurion and supercovariant derivatives acting on it. Comparing (4.11) with (4.9) yields the relation (4.3).

It is evident that the  $\theta^2$  term in (4.8) yields the gaugino mass, and (4.10) agrees with the result of [16], quoted above in (2.10). This result for  $M_a$  agrees with (4.1), as seen from (4.2) and the contribution of the log  $\Lambda$  term in (2.7) to  $\tilde{C}_{susy}$ . The expression for  $m_{\tilde{f}}^2$ quoted above in (4.1) follows from (4.3) and the result (2.10).

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